

# Heterogeneous Agents in Macro Models

Creative Destruction and Uncertainty

Petr Sedláček

Lake Como School of Advanced Studies

July 2018

# Starting point: Uncertainty rises in recessions

## Dominant view in the literature

- exogenous uncertainty increases cause recessions
  - ▶ e.g. Bloom (2009), Christiano et al. (2010), Schaal (2015)

**This paper:** think about uncertainty related to innovation and growth

- 1. why and how is growth related to uncertainty?
- 2. can such “growth-driven” uncertainty be *counter*-cyclical?
- 3. to what extent is uncertainty in the data driven by growth?

# This paper: structural model

In all what follows, I focus on *firm-level* uncertainty

- cross-sectional dispersion of firm-level TFP (Bloom et al., 2014)

Tractable general equilibrium model of endogenous firm dynamics

- firms differ in productivity levels
  - ▶ can invest in improving technology
  - ▶  $\uparrow$  tech. investment  $\rightarrow$   $\uparrow$  chances of adopting better technology vintages
- endogenous entry, exit and employment decisions

1. Why/how is technology growth related to firm-level uncertainty?

- innovation is uncertain and faster growth leads to
  - ▶ larger productivity gains (losses) if innovation is (not) successful

# This paper: structural model

## 2. Can such growth-driven uncertainty be *counter-cyclical*?

- faster technology growth spurs a process of creative destruction
  - ▶ firms at the frontier expand and shut down less often
  - ▶ firms below the frontier become more obsolete, shrink and shut down
- → simultaneous increase in job creation and job destruction
  - ▶ in calibrated model destruction dominates → Schumpeterian downturn
  - ▶ → growth-driven uncertainty is counter-cyclical

# This paper: empirical evidence

## 3. To what extent is uncertainty growth-driven in the data?

- estimate series of structural VARs with long-run restrictions
- positive technology shocks lead to
  - ▶ an increase in R&D, job creation and job destruction
  - ▶ a temporary drop in aggregate employment
  - ▶ an increase in firm-level uncertainty
- quantify extent of uncertainty variation driven by technology shocks
  - ▶ on average technology shocks explain 27 percent
  - ▶ certain periods more important (70% around dot-com bubble recession)
  - ▶ certain periods less important (Great Recession unrelated to growth)

# Related literature

## Uncertainty shocks and their effects

- Bloom (2009), Christiano, Motto, Rostagno (2010), Arellano, Bai, Kehoe (2012), Bloom et al. (2012), Schaal (2012), Bachmann, Born, Elstner, Grimme (2013), Bachmann, Bayer (2014), Caggiano, Castelnuovo, Groshenny (2014), Vavra (2014), Jurado et al. (2015)

## Model of creative destruction and technology adoption

- Aghion, Howitt (1994), Caballero, Hammour (1996), Mortensen, Pissarides (1998), Gali (1999), Klette, Kortum (2004), Fisher (2006), Lopez-Salido, Michelacci (2007), Comin, Gertler, Santacreu (2009), Buera, Oberfield (2015), Akcigit, Kerr (2016)

## Endogenous fluctuations in uncertainty

- Bachmann, Moscarini (2012), Gourio (2014), Orlik, Veldkamp (2014), Plante et al. (2014), D'Erasmus et al. (2015), Ludvigson et al. (2016)

# **Nexus of growth, business cycles and uncertainty?**

(Structural model)

# Household preferences and choices

## Utility-maximizing representative household

- chooses consumption ( $C_t$ ) and labor supply ( $N_t$ )

$$\max_{\{C_t, N_t\}_0^\infty} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t (\ln C_t - \zeta N_t)$$

$$C_t = W_t N_t + \Pi_t$$

- $W_t$  is competitive wage rate and  $\Pi_t$  are firm profits
- optimal labor supply implies

$$W_t = \zeta C_t$$



# Technology growth and technology investment

Exogenous stochastically growing technological frontier

$$\ln Z_t = \bar{Z} + \ln Z_{t-1} + \epsilon_{Z,t}$$

- $\bar{Z} > 0$ : average technology growth
- $\epsilon_{Z,t} \sim N(0, \sigma_Z^2)$ : technology shocks

Firms endogenously adopt newer technology

- investing  $r$  units of final good results in  $p$  probability of innovating

$$p = \left( \frac{r}{\chi} \right)^{1/\eta} \gamma^{1-1/\eta}$$

- ▶  $\gamma = z/Z$ : relative “stock of knowledge” (distance from frontier)
- ▶  $1/\eta$ : elasticity of tech. adoption “production function”

## Firm-level productivity

Given tech. expenditures, incumbent firm with technology vintage of age  $j$

- ① retains its previous productivity level if it fails to innovate
- ② attains younger vintage of technology if it innovates
  - ▶  $\theta$  share of innovations are *radical*  $\rightarrow$  attain leading technology
  - ▶ remaining innovations are *incremental*  $\rightarrow$  attain closest younger vintage

$$\ln z_{j,t} \rightarrow \begin{cases} \ln z_{j+1,t+1} & \text{with probability } 1 - p_{j,t}, \\ \ln z_{j,t+1} & \text{with probability } p_{j,t}(1 - \theta), \\ \ln Z_{t+1} & \text{with probability } p_{j,t}\theta \end{cases}$$

Tech. investment conducted also by potential entrants

- assume that only those with radical innovations successfully start up

# Firm dynamics: entry, growth and exit

- firm entry
  - ▶ free entry of radically innovating startups
- employment choices conditional on firm-level productivity
  - ▶ incumbent production function  $y_{i,t} = A_t z_{i,t} n_{i,t}^\alpha$
- firm life-cycle growth
  - ▶ efficiency gains from learning-by-doing  $\psi_a$
- firm exit
  - ▶ payment of stochastic idiosyncratic operational costs  $\phi$

$$\mathbb{V}_a(z_{i,t}, \mathcal{F}_t) = \max_{n_{i,a,t}, p_{i,a,t}, \tilde{\phi}_{i,a,t}} \int^{\tilde{\phi}_{i,a,t}} \left[ \begin{array}{l} y_{i,a,t} + \psi_{a,t} n_{i,a,t} - W_t n_{i,a,t} \\ - R(p_{i,a,t}, \gamma_{i,t}) - \phi \\ + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \mathbb{V}_{a+1}(z_{i,t+1}, \mathcal{F}_{t+1}) \end{array} \right] dH_t(\phi)$$

# Firm productivity (size) distribution and its evolution

- $\omega_{j,a,t}$ : mass of firms of age  $a$  and technology vintage  $j$  years old
- $\bar{E}$ : fixed mass of potential startups

$$\omega_{0,0,t} = \bar{E} p_{e,t} \theta$$

$$\omega_{0,a+1,t+1} = \begin{cases} \sum_j \sum_a \int^{\tilde{\phi}_{j,a,t}} p_{j,a,t} \theta \omega_{j,a,t} dH(\phi) & j = 0, 1, 2, \dots, \\ & a = 0, 1, 2, \dots, \\ \int^{\tilde{\phi}_{0,a,t}} p_{0,a,t} (1 - \theta) \omega_{0,a,t} dH(\phi) & j \leq a, \end{cases}$$

$$\omega_{j+1,a+1,t+1} = \sum_j \sum_a \left[ \begin{array}{l} \int^{\tilde{\phi}_{j,a,t}} (1 - p_{j,a,t}) \omega_{j,a,t} dH(\phi) + \\ \int^{\tilde{\phi}_{j+1,a,t}} p_{j+1,a,t} (1 - \theta) \omega_{j+1,a,t} dH(\phi) \end{array} \right] \begin{array}{l} j = 0, 1, 2, \dots, \\ a = 0, 1, 2, \dots, \\ j \leq a, \end{array}$$

## Firm-level uncertainty: measurement

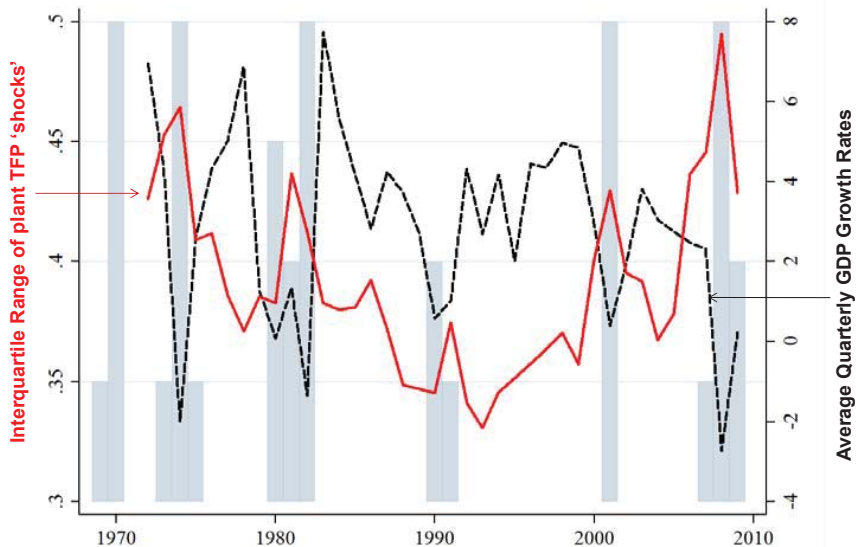
Follow Bloom et al. (2014): dispersion of establishment-level TFP shocks

- define productivity *shocks* from

$$\ln \hat{z}_{i,t} = \rho \ln \hat{z}_{i,t-1} + \mu_i + \lambda_t + v_{i,t}$$

- ▶  $\mu_i$ : establishment fixed-effects
  - ▶  $\lambda_t$ : time fixed-effects
  - ▶  $v_{i,t}$ : establishment-level TFP shocks with time-varying variance  $\sigma_t^2$
- uncertainty ( $\sigma_t$ ) measured as cross-sectional dispersion of TFP shocks

# Firm-level uncertainty: measurement



Source: Bloom et al. (2012).

# 1. Why is growth linked to uncertainty in the model?

Consider simplified version of innovation process

- assume  $p_{i,t} = p$  and  $\theta = 1$

In a large enough cross-section of firms

- fraction  $p$  of firms adopt the leading technology  $Z_t$
- fraction  $1 - p$  retain their previous productivity levels

Individual firm productivity can then, on average, be described by

$$\ln z_{i,t} = (1 - p) \ln z_{i,t-1} + p \ln Z_t + v_{i,t}$$

- with  $\mathbb{E}[v_{i,t}] = 0$

# 1. Why is growth linked to uncertainty in the model?

Consider simplified version of innovation process

- assume  $p_{i,t} = p$  and  $\theta = 1$

In a large enough cross-section of firms

- fraction  $p$  of firms adopt the leading technology  $Z_t$
- fraction  $1 - p$  retain their previous productivity levels

Individual firm productivity can then, on average, be described by

$$\ln z_{i,t} = \rho \ln z_{i,t-1} + \lambda_t + v_{i,t}$$

- with  $\mathbb{E}[v_{i,t}] = 0$ ,  $\rho = (1 - p)$  and  $\lambda_t = p \ln Z_t$



# 1. Why is growth linked to uncertainty in the model?

Firm-level uncertainty measured as cross-sectional variance of TFP shocks

$$v_{i,t} = \omega_{i,t}(p-1)(\ln \gamma_{i,t-1} - \bar{Z}) + (1-\omega_{i,t})p(\ln \gamma_{i,t-1} + \bar{Z})$$

- $\omega_{i,t}$ : is an indicator function

- ▶  $\omega_{i,t} = 1$  with probability  $p$  and 0 otherwise

$$\sigma_t^2 = \text{var}[v_{i,t}] = p[(1+p)\sigma_\gamma^2 + (1-p)\mu_\gamma] + p(1-p)\bar{Z}^2$$

- where uncertainty depends on

- ▶ uncertainty depends on innovation speed ( $p$ )
- ▶ productivity distribution ( $\mathbb{E}[\ln \gamma_{i,t}] = \mu_\gamma$  and  $\text{var}[\ln \gamma_{i,t}] = \sigma_\gamma^2$ )
- ▶ speed of technology growth  $\bar{Z}$

# 1. Why is growth linked to uncertainty in the model?

Firm-level uncertainty measured as cross-sectional variance of TFP shocks

$$v_{i,t} = \omega_{i,t}(p-1)(\ln \gamma_{i,t-1} - \bar{Z}) + (1 - \omega_{i,t})p(\ln \gamma_{i,t-1} + \bar{Z})$$

- $\omega_{i,t}$ : is an indicator function

- ▶  $\omega_{i,t} = 1$  with probability  $p$  and 0 otherwise

$$\sigma_t^2 = \text{var}[v_{i,t}] = p[(1+p)\sigma_\gamma^2 + (1-p)\mu_\gamma] + p(1-p)\bar{Z}_t^2$$

- where uncertainty depends on

- ▶ uncertainty depends on innovation speed ( $p$ )
- ▶ productivity distribution ( $\mathbb{E}[\ln \gamma_{i,t}] = \mu_\gamma$  and  $\text{var}[\ln \gamma_{i,t}] = \sigma_\gamma^2$ )
- ▶ speed of technology growth  $\bar{Z} \rightarrow \sigma_t^2$  rises with  $\bar{Z}_t$

## Parametrization, model performance and results

# Calibration: main model features and related targets

- operational costs distribution: average exit
- learning-by-doing efficiency gains: average size by age
- tech. adoption parameters: estimates from Akcigit, Kerr (2015)
- aggregate shocks: cyclical patterns of output and R&D data

# Model matches reallocation and R&D patterns in data

## Firm shares and size distributions

- many young firms are small (BDS)

## Reallocation process

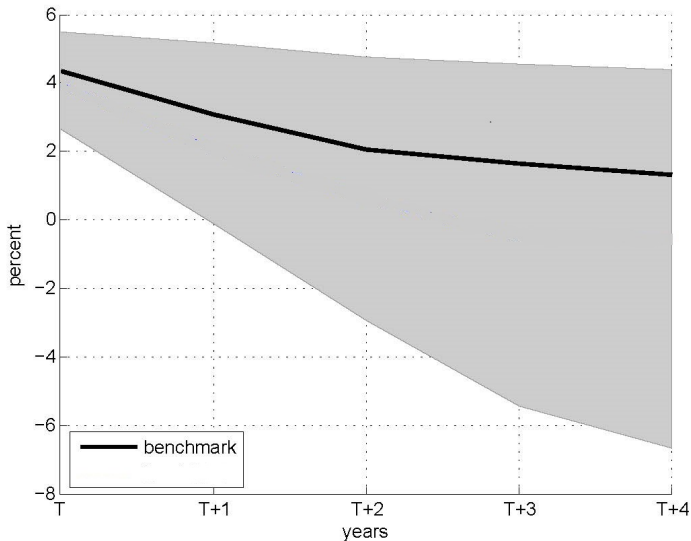
- lots of churn, largely driven by entry and exit (BDS)

## Technology expenditures at the firm level

- small firms innovate relatively more in data
- R&D positively correlated with productivity level
- less so with productivity growth

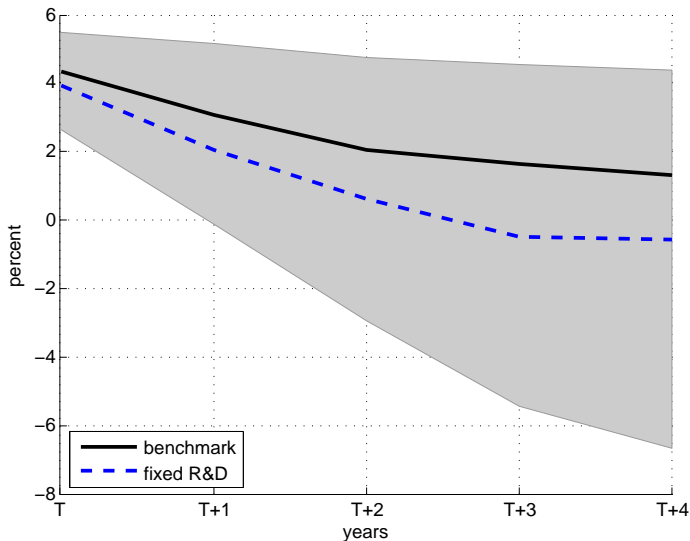
# 1. How is technology growth linked to uncertainty?

Measuring uncertainty as in Bloom et al. (2014)



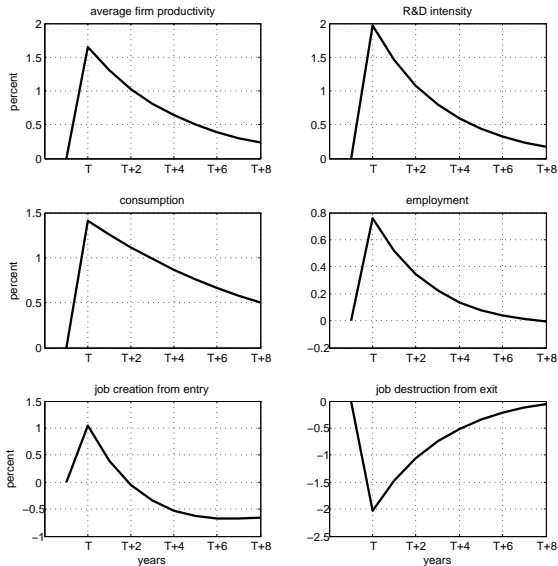
# 1. How is technology growth linked to uncertainty?

Measuring uncertainty as in Bloom et al. (2014)



## 2. Can growth-driven uncertainty be counter-cyclical?

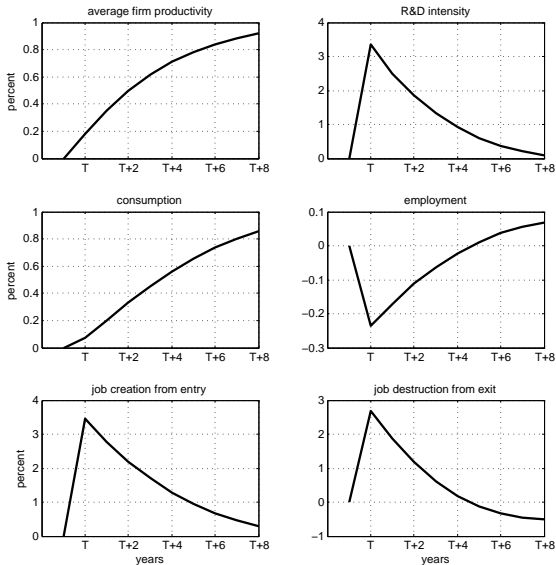
Aggregate dynamics following a positive aggregate TFP shock





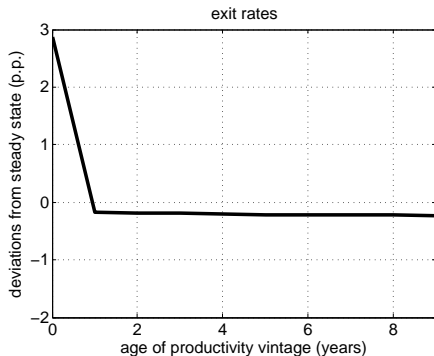
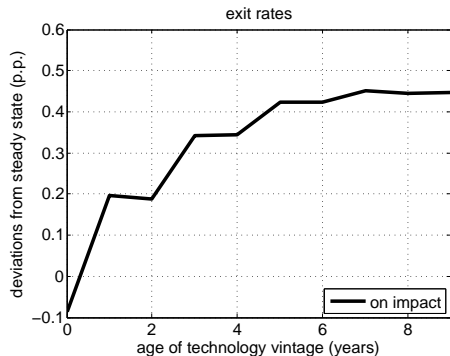
## 2. Can growth-driven uncertainty be counter-cyclical?

Aggregate dynamics following a positive technology shock



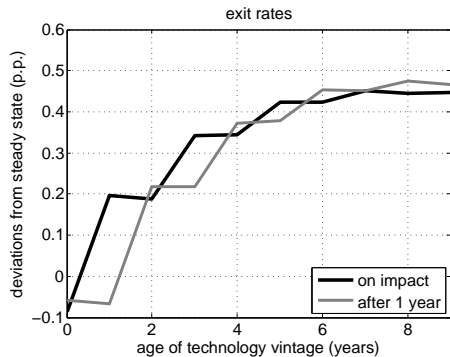
## 2. Can growth-driven uncertainty be counter-cyclical?

Distributional dynamics following a positive technology shock



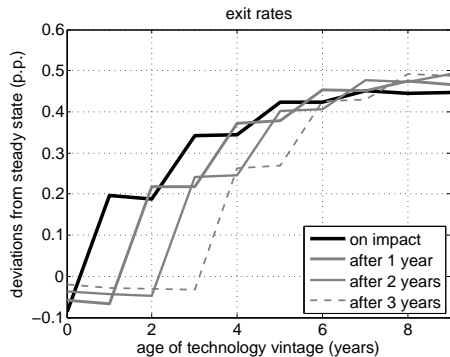
## 2. Can growth-driven uncertainty be counter-cyclical?

Distributional dynamics following a positive technology shock



## 2. Can growth-driven uncertainty be counter-cyclical?

Distributional dynamics following a positive technology shock



## 2. Can growth-driven uncertainty be counter-cyclical?

Unconditional cyclical of firm-level uncertainty in model

- simulate economy 1,000 times for 1,040 periods
- shocks distributed according to calibrated values
- drop first 1,000 periods

	output	employment	frontier tech.
		<i>model</i>	
$\text{corr}(\sigma_t, x_t)$	-0.19 [-0.37, -0.01]	-0.13 [-0.31, 0.05]	0.35 [0.17, 0.53]
		<i>data</i>	
$\text{corr}(\sigma_t, x_t)$	-0.46	-0.42	0.33

**To what extent is uncertainty growth-driven in the data?**  
(testing the model's predictions)

# Technology shocks, firm dynamics and uncertainty

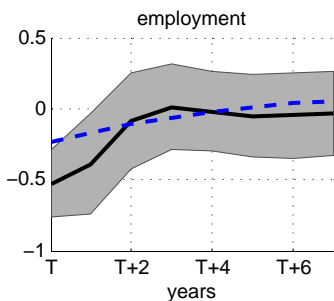
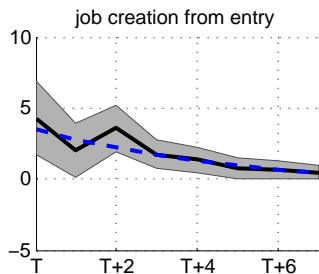
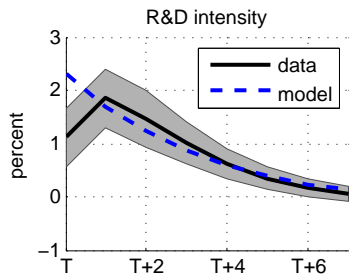
Estimate series of structural VARs with long-run restrictions

- following Blanchard, Quah (1989), Gali (1999)
- only technology shocks affect productivity in long-run
- include firm-dynamics, R&D and uncertainty in data vector

Similar results obtained with alternative estimation strategy

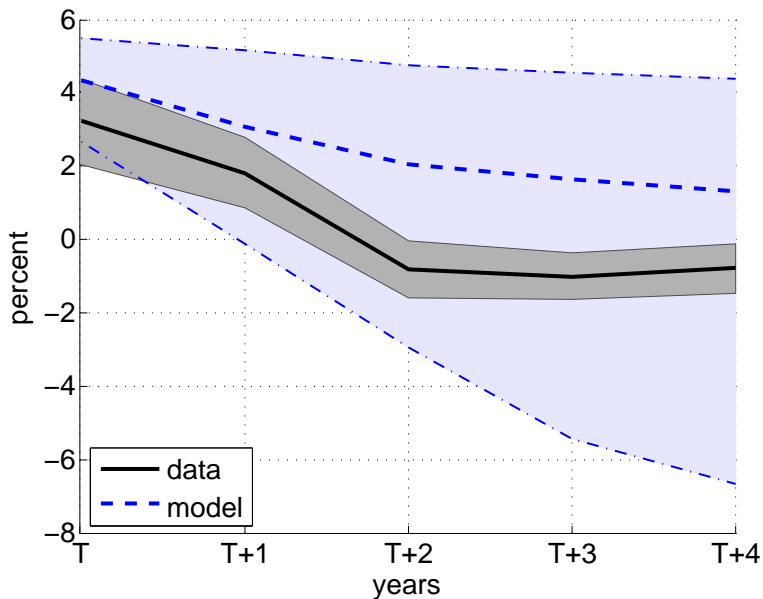
- local projections and Basu et al. (2013) technology shocks

# Technology shocks, firm dynamics and uncertainty



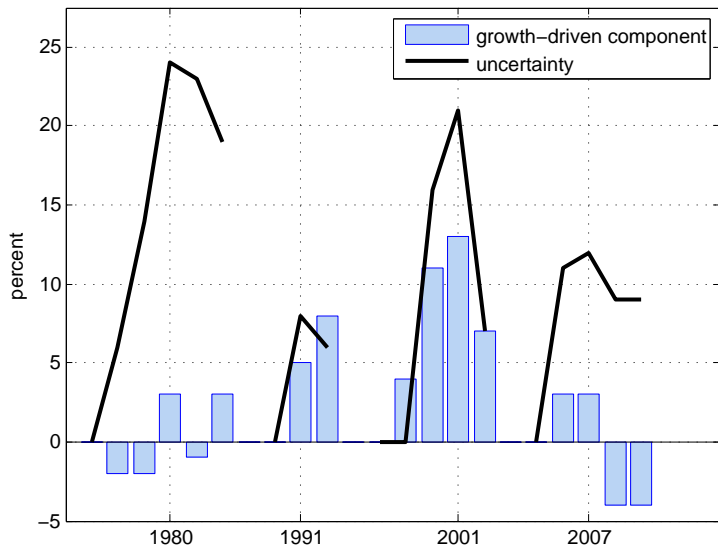


# Technology shocks, firm dynamics and uncertainty



### 3. To what extent is uncertainty growth-driven in data?

On average, technology shocks explain 27% of uncertainty variation



# Summary

Structural model linking growth, business cycles and uncertainty

- technology improvements spur creative destruction process
- at the same time, firm-level uncertainty increases
- → counter-cyclical uncertainty fluctuations

Model predictions are consistent with the data

- establishment dynamics following technology shocks
- uncertainty increases following positive technology shocks

Role of growth-driven uncertainty in data

- on average accounts for 30% of observed uncertainty variation
- particularly important in the 90's and around the new millennium

**Thanks**

# Model details

Firm maximization problem:

$$\mathbb{V}_a(z_{i,t}, \mathcal{F}_t) = \max_{n_{i,a,t}, p_{i,a,t}, \tilde{\phi}_{i,a,t}} \int^{\tilde{\phi}_{i,a,t}} \left[ \begin{array}{l} y_{i,a,t} + \psi_{a,t} n_{i,a,t} - W_t n_{i,a,t} \\ - R(p_{i,a,t}, \gamma_{i,t}) - \phi \\ + \mathbb{E}_t \beta \frac{C_t}{C_{t+1}} \mathbb{V}_{a+1}(z_{i,t+1}, \mathcal{F}_{t+1}) \end{array} \right] dH_t(\phi)$$

# Household preferences and choices

## Utility-maximizing representative household

- chooses consumption ( $C_t$ ) and labor supply ( $N_t$ )

$$\max_{\{C_t, N_t\}_0^\infty} \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t (\ln C_t - \zeta N_t)$$

$$C_t = W_t N_t + \Pi_t$$

- $W_t$  is competitive wage rate and  $\Pi_t$  are firm profits
- optimal labor supply implies

$$W_t = \zeta C_t$$

# Firm productivity (size) distribution and its evolution

- $\omega_{j,a,t}$ : mass of firms of age  $a$  and technology vintage  $j$  years old
- $\bar{E}$ : fixed mass of potential startups

$$\omega_{0,0,t} = \bar{E} p_{e,t} \theta$$

$$\omega_{0,a+1,t+1} = \begin{array}{ll} \sum_j \sum_a \int^{\tilde{\phi}_{j,a,t}} p_{j,a,t} \theta \omega_{j,a,t} dH(\phi) & j = 0, 1, 2, \dots, \\ & a = 0, 1, 2, \dots, \\ \int^{\tilde{\phi}_{0,a,t}} p_{0,a,t} (1 - \theta) \omega_{0,a,t} dH(\phi) & j \leq a, \end{array}$$

$$\omega_{j+1,a+1,t+1} = \sum_j \sum_a \left[ \begin{array}{l} \int^{\tilde{\phi}_{j,a,t}} (1 - p_{j,a,t}) \omega_{j,a,t} dH(\phi) + \\ \int^{\tilde{\phi}_{j+1,a,t}} p_{j+1,a,t} (1 - \theta) \omega_{j+1,a,t} dH(\phi) \end{array} \right] \begin{array}{l} j = 0, 1, 2, \dots, \\ a = 0, 1, 2, \dots, \\ j \leq a, \end{array}$$

back

# Model parameters

	parameter	value	target/source
$\beta$	discount factor	0.97	annual interest rate 3%
$v$	disutility of worker labor	3.633	wage normalization, $W_{ss} = 1$
$\chi$	R&D normalizing constant	0.280	firm productivity persistence 0.79, Foster et al. 2008
$\eta$	R&D cost curvature	2	patent elasticity w.r.t R&D 0.5, Acemoglu et al. 2013
$\theta$	probability of radical innovation	0.1	Akcigit and Kerr (2016)
$\alpha$	returns to scale	0.670	labor share 66%
$\psi_s$	learning-by-doing efficiency gains, startups	-0.545	rel. average size of startups 52%, BDS
$\psi_y$	learning-by-doing efficiency gains, young establishments	-0.344	rel. average size of young establishments 72%, BDS
$\psi_m$	learning-by-doing efficiency gains, medium-aged establishments	-0.195	rel. average size of medium-age establishments 90%, BDS
$\psi_o$	learning-by-doing efficiency gains, old establishments	0	normalization
$\mu_H$	operational cost mean	0.093	0 average paid operational costs, normalization
$\sigma_H$	operational cost distribution, scale	0.238	average establishment exit rate of 11%, BDS
$\bar{E}$	mass of potential entrants	8.883	firm mass of 1, normalization
$Z$	frontier technology drift	0.016	average patent application growth, USPTO
$\sigma_Z$	frontier technology shocks, standard deviation	0.010	corr(R&D,Y)=0.21, BEA
$\rho_A$	aggregate TFP shock, persistence	0.788	real GDP autocorrelation 0.79, BEA
$\sigma_A$	aggregate TFP shock, volatility	0.016	real GDP volatility 0.016, BEA



## Firm distributions

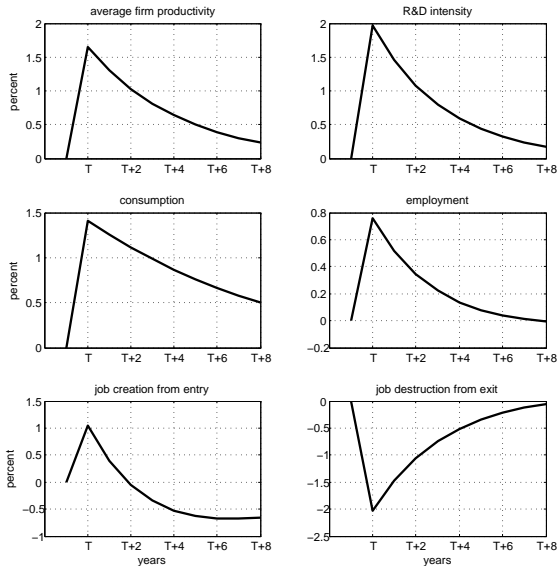
---

	establishment age			
	0	1-5	6-10	11+
	<i>establishment shares</i>			
data	11	32	19	38
model	12	35	21	32
	<i>employment shares</i>			
data	5	23	17	55
model	6	25	19	50

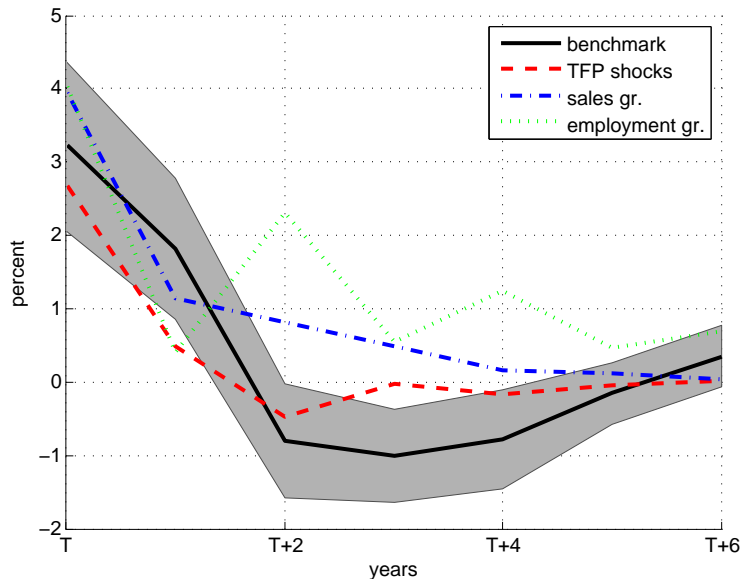
---

## 2. Can growth-driven uncertainty be counter-cyclical?

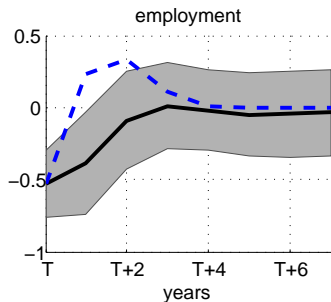
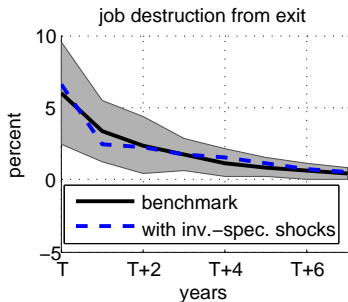
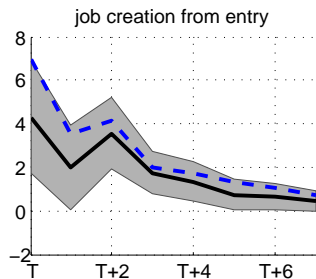
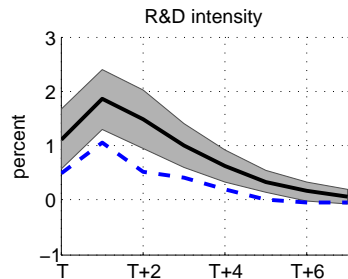
Aggregate dynamics following a positive aggregate TFP shock



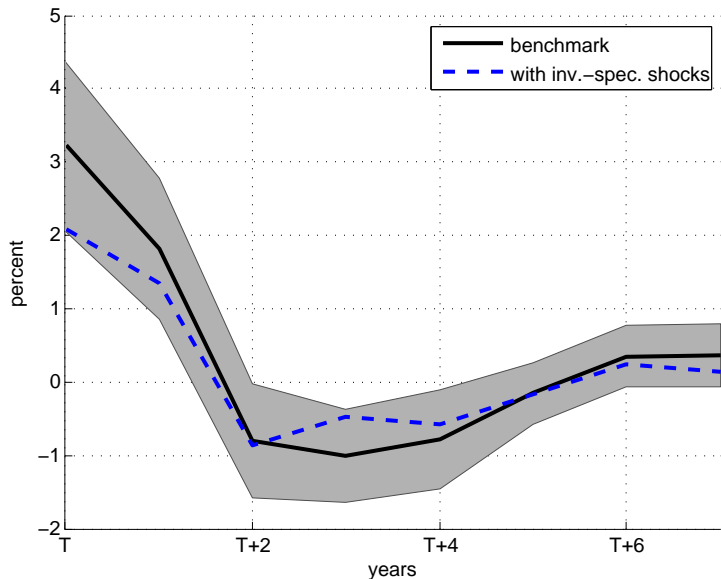
# Alternative uncertainty measures



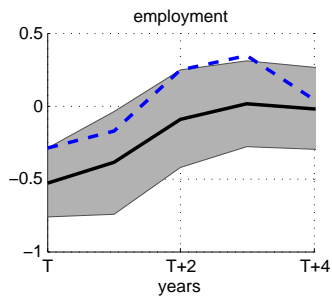
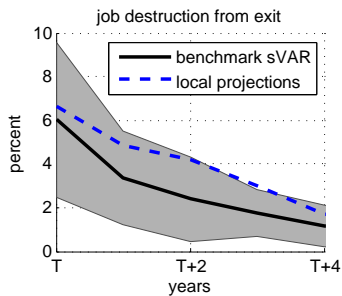
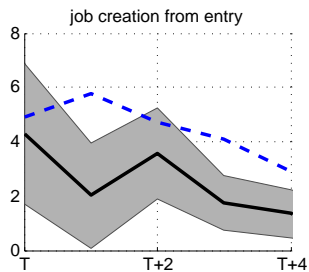
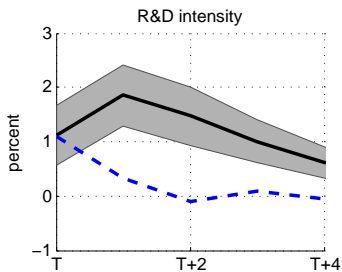
# Accounting for investment-specific shocks



# Accounting for investment-specific shocks



# Alternative estimation strategy



# Alternative estimation strategy

